

Introducing Number Theory in the Elementary Classroom

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Prime and Composite Numbers

College Level Definitions:

Prime: Let p be in the element of natural numbers. p is prime if its only positive factors are 1 and p .

Composite: Let n be in the element of natural numbers. n is composite if it has at least one positive factor other than 1 and n .

Elementary School Definitions:

Prime: A number that can be divided by only the number 1 and itself.

Composite: Any number that is divisible by itself, 1, and another number.

Prime

2 is prime because



$2 = 1 \times 2$

3 is prime because



$3 = 1 \times 3$

They can **ONLY** be divided by the number 1 and itself.

Composite

6 is composite because



$6 = 3 \times 2$



$6 = 1 \times 6$

AND

Fibonacci Numbers

College Level Definition: The Fibonacci Sequence is defined by $F_1 = 1, F_2 = 1, F_n = F_{n-1} + F_{n-2}$, for n is greater than or equal to 3.

Elementary School Definition: The Fibonacci Sequence is a series of numbers that start with 0 and 1, and then each new number is created by adding the two numbers that come before it.



Fun Fact: Fibonacci Numbers can often be found on many things in nature, including this pineapple! These pictures show the same pineapple being rotated; the labels are counting the number of spiral patterns shown on this pineapple. By counting the number of spiral columns around the pineapple, I found that there are 8 spirals, which is a Fibonacci Number!

How?

The Fibonacci Sequence is 1, 1, 2, 3, 5, 8, 13, 21, etc.

To find the next number, just add the previous two numbers together!

Even and Odd Numbers

College Level Definitions:

Even: Any integer that can be written in the form $2k$, where k is also an integer.

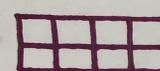
Odd: An integer that cannot be divided evenly by 2. An integer n can be expressed as $n = 2k + 1$, where k is an integer.

Elementary School Definitions:

Even: A number that can be split into equal groups with nothing left over. In other words, a number that is divisible by 2.

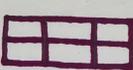
Odd: A number that cannot be split into equal groups. In other words, a number that is not divisible by 2.

Even

8 = 

8 is **even** because

$8 = 2(4)$
or
 $8 \div 2 = 4$

6 = 

6 is **even** because

$6 = 2(3)$
or
 $6 \div 2 = 3$

Odd

7 = 

7 is **odd** because

$7 = 2(3) + 1$
or
7 is **NOT** divisible by 2

5 = 

5 is **odd** because

$5 = 2(2) + 1$
or
5 is **NOT** divisible by 2

Euclidean Algorithm:

Finding the **greatest common divisor (gcd)** of two numbers.

gcd: Let a and b be integers that are not both equal to 0. The greatest common divisor of a and b is the largest d in the element of natural numbers for which d divides a and d divides b .

We express this in symbols as $d = \text{gcd}(a, b)$.

Euclidean Algorithm

$\text{gcd}(28, 36)$

$$36 = 1 \times 28 + 8$$

$$28 = 3 \times 8 + 4$$

$$8 = 2 \times 4 + 0$$

So, the greatest common divisor of 28 and 36

is **4**

$\text{gcd}(234, 540)$

$$540 = 2 \times 234 + 72$$

$$234 = 3 \times 72 + 18$$

$$72 = 4 \times 18 + 0$$

So, the greatest common divisor of 234 and 540

is **18**

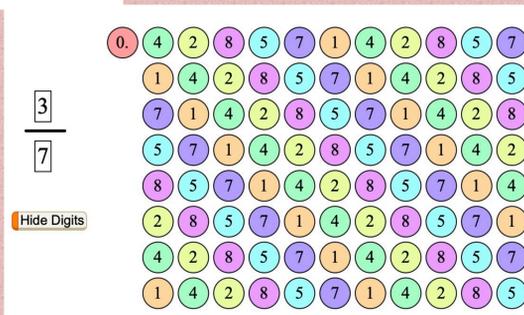
Rational Numbers

College Level Definition: We define the set of rational numbers by $Q =$ the set of a/b such that a, b is an element of integers and b cannot be 0.

Elementary School Definition: A real number that can be written as a fraction, where both the numerator and the denominator are integers, and the denominator is not zero.



We can see some cool patterns within some rational numbers, using their decimal and color-coded numbers!



Factoring into Primes:

Fundamental Theorem of Arithmetic:

Every positive integer (except the number 1) can be represented uniquely as a product of one or more primes.

Factor Trees

How to find all factors

28

14 2

7 2

$28 = 2 \cdot 2 \cdot 7$
 $28 = 2^2 \cdot 7$

1 2 4 7 14 28

36

6 6

3 2 3 2

$36 = 3 \cdot 2 \cdot 3 \cdot 2$
 $36 = 3^2 \cdot 2^2$

1 2 3 4 6 9 12 18 36